

1.) Find the general solution to the system of equations

a)

$$\begin{aligned}x_1'(t) &= 3x_1 - 2x_2 \\x_2'(t) &= 2x_1 - 2x_2\end{aligned}$$

b)

$$\begin{aligned}x_1'(t) &= 3x_1 - 2x_2 \\x_2'(t) &= 4x_1 - 1x_2\end{aligned}$$

c)

$$\begin{aligned}x_1'(t) &= 3x_1 - 4x_2 \\x_2'(t) &= x_1 - 1x_2\end{aligned}$$

d)

$$\begin{aligned}x_1'(t) &= x_1 + 2x_2 \\x_2'(t) &= -5x_1 - 1x_2\end{aligned}$$

2.) Solve the initial value problems

$$\begin{array}{ll} \text{a) } \vec{x}' = \begin{pmatrix} -2 & 1 \\ -5 & 4 \end{pmatrix} \vec{x}, & \vec{x}_0 = \begin{pmatrix} 1 \\ -3 \end{pmatrix} & \text{b) } \vec{x}' = \begin{pmatrix} 1 & -5 \\ 1 & -3 \end{pmatrix} \vec{x}, & \vec{x}_0 = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ \text{c) } \vec{x}' = \begin{pmatrix} 2 & \frac{3}{2} \\ -\frac{3}{2} & -1 \end{pmatrix} \vec{x}, & \vec{x}_0 = \begin{pmatrix} 3 \\ -2 \end{pmatrix} & \text{d) } \vec{x}' = \begin{pmatrix} 3 & 9 \\ -1 & -3 \end{pmatrix} \vec{x}, & \vec{x}_0 = \begin{pmatrix} 2 \\ 4 \end{pmatrix} \end{array}$$